6.004 Tutorial Problems
L04 – Procedures and Stacks II

RISC-V Calling Conventions:

- Caller places arguments in registers a0–a7
- Caller transfers control to callee using jal (jump-and-link) to capture the return address in register ra. The following three instructions are equivalent (pc stands for program counter, the memory address of the current/next instruction):
  - jal ra, label: R[ra] <= pc + 4; pc <= label
  - jal label (pseudoinstruction for the above)
  - call label (pseudoinstruction for the above)

- Callee runs, and places results in registers a0 and a1
- Callee transfers control to caller using jr (jump-register) instruction. The following instructions are equivalent:
  - jalr x0, 0(ra): pc <= R[ra]
  - jr ra (pseudoinstruction for the above)
  - ret (pseudoinstruction for the above)

Stack discipline: can put anything on the stack, but leave stack the way you found it

Always save s registers before using them
Save a and t registers if you need their value after procedure call returns.
Always save ra if making nested procedure calls.
RISC-V Stack

- Stack is in memory \( \rightarrow \) need a register to point to it
  - In RISC-V, stack pointer sp is \( x2 \)

- Stack grows down from higher to lower addresses
  - Push decreases sp
  - Pop increases sp

- sp points to top of stack (last pushed element)

- Discipline: Can use stack \textit{at any time}, but leave it as you found it!

Using the stack

Sample entry sequence

```assembly
addi sp, sp, -8
sw ra, 0(sp)
sw a0, 4(sp)
```

Corresponding Exit sequence

```assembly
lw ra, 0(sp)
lw a0, 4(sp)
addi sp, sp, 8
```
Note: A small subset of essential problems are marked with a red star (★). We especially encourage you to try these out before recitation.

Problem 1.

Write assembly program that computes square of the sum of two numbers (i.e. squareSum(x,y) = (x + y)^2) and follows RISC-V calling convention. Note that in your assembly code you have to call assembly procedures for mult and sum. They are not provided to you, but they are fully functional and obey the calling convention.

```c
/* compute square sum of args */
unsigned squareSum(unsigned x, unsigned y) {
    unsigned z = sum(x, y);
    return mult(z, z);
}
```

```
squareSum:
    addi sp, sp, -4   // adjust stack pointer
    sw ra, 0(sp)     // Store ra since it will be overwritten
    jal sum          // same as jal ra, sum: call sum(x, y)
    mv a1, a0        // copy the result of sum to a1
    jal mult         // same as jal ra, mult: call mult(sum(...),
                   // sum(...))
    lw ra, 0(sp)     // restore ra
    addi sp, sp, 4   // adjust stack pointer
    ret
```
Problem 2. ★

The following C program computes the log base 2 of its argument. The assembly code for the procedure is shown on the right, along with a stack trace showing the execution of ilog2(10). The execution has been halted just as it’s about to execute the instruction labeled “rtn:” The SP label on the stack shows where the SP is pointing to when execution halted.

```c
/* compute log base 2 of arg */
int ilog2(unsigned x) {
    unsigned y;
    if (x == 0) return 0;
    else {
        /* shift x right by 1 bit */
        y = x >> 1;
        return ilog2(y) + 1;
    }
}
```

(A) Please fill in the values for the two blank locations in the stack trace shown on the right. Please express the values in hex.

**Fill in values (in hex!) for 2 blank locations**

By analyzing the program’s assembly code, we can that in each iteration the stack pointer is decremented by 8, and then the values of s0 and ra are stored in the two words that were just allocated. Since we’re about to execute the ‘jr ra’ instruction, we just loaded ra and s0 off the stack, and then added 8 to the stack pointer. Thus, the two blanks must be the s0 and ra the current function call saved to the stack originally.

If we work backwards from ‘jr ra’, we see that we also must have come back from a recursive call to ilog2, given the ‘jal ra, ilog2’. Thus, the two slots above the blanks are the s0 and ra of that recursive call. This gives us some more info, that the address of the ‘addi a0, a0, 1’ instruction is 0x240, and that the recursive call is given 0x1 as its argument, which can be deduced by seeing that the argument a0 is just copied from s0 right before the recursive call. In each recursive call, a0 is shifted to the right by one, so in the current function call, the value of a0 must have been 0x2 or 0x3. Since the original call had an argument of 10, we are also in a recursive call! This means the ra that we save to the stack is also 0x240, hence the first blank.

Finally, we can go to the two slots below the blanks to see what our parent call placed there. Since it placed 0x5 as s0’s saved value, our argument would have been 0x5 >> 1, or 0x2. This gives us the second blank.
(B) What are the values in a0, s0, sp, and pc at the time execution was halted? Please express the values in hex or write “CAN’T TELL”.

Value in a0: 0x___________  in s0: 0x___________
Value in sp: 0x___________  in pc: 0x___________

a0 = 2, s0 = 2, sp = Can’t tell, pc = 0x250

To find a0, we need to know where the base case occurred. We know the two slots above the blank are for the next recursive call. Since it has an argument of 1, its next recursive call gets an argument of 0, meaning it skips recursing and just returns. The function returns to our child call, which adds 1 to a0 and then returns to our current call, which also adds 1 to a0. Thus, a0 = 2.

We know we just loaded s0 back from the stack, so we can work backward to see should “un-add” 8 to see where the stack was, then load s0 from 4 after, which points to the blank which we filled with 0x2. At no point in the program does the value of sp get saved to the stack, so there’s no way for us to tell where the stack lives in memory.

Since we know that the return address of the recursive call is 0x240, we can count forward instruction by instruction, adding 0x4 each time to find the pc of the ‘jr ra’ instruction, which is at 0x250

(C) What was the address of the original ilog2(10) function call?

Original ilog2(10) address: 0x___________

0x1104

We know that the two stack entries 0x240 and 0x5 were from the current call’s parent call. Since its argument was thus 0x5, it still is not the original call. Thus, the next two entries must be from its parent call. However, we now find completely different values for s0 and ra. This must mean that these were the values saved when ilog2 started running, since the ra of 0x1108 points to some distant other part of memory. We can then tell that this is the data saved by the original call. If the return address of that original call is 0x1108, then the original call occurred at 0x1104, since it added 4 to its PC to get the return address.
Problem 3. ★

You are given an incomplete listing of a C program (shown below) and its translation to RISC-V assembly code (shown on the right):

```c
int fn(int x) {
    int lowbit = x & 1;
    int rest = x >> 1;
    if (x == 0) return 0;
    else return ???;
}
```

(A) What is the missing C source corresponding to ??? in the above program?

**C source code:** ________________________________

```
fn(rest) + lowbit
```

By taking a close look at the assembly, we can see that s0 is set to \( x \& 1 \), since the first argument \( x \) is located in the a0 register. Thus, s0 contains ‘lowbit’. The same can be done for s1, which contains ‘rest’. On the line labeled ‘yy’, we branch forward to ‘rtn’ if a0, or \( x \), is equal to 0. Thus, ‘rtn’ should correspond to the ‘then’ block of the if in the source code, and ‘yy’ corresponds to the ‘else’ block. In ‘yy’, we recursively call fn with s1 moved into a0 for the argument, then add s0 to the result. In the source code, this corresponds to \( fn(rest) + lowbit \). Then from here, the program just cleans up and returns, so this is the result.
The procedure \texttt{fn} is called from an external procedure and its execution is interrupted just prior to the execution of the instruction tagged ‘\texttt{yy}’. The contents of a region of memory during one of the recursive calls to \texttt{fn} are shown on the left below. If the answer to any of the below problems cannot be deduced from the provided information, write “CAN’T TELL”.

From the context we can learn a lot of information about what’s on the stack. If we look backwards a bit from the point that execution is stopped, we see that we just recently subtracted 12 from sp, which allocated 3 words of space on the stack, and then stored s0, s1, and ra there. Thus, sp currently points to the first of those 3 words stored.

Additionally, since execution was stopped prior to the ‘jal ra, fn’ recursive call, the 3 words above the current sp are junk, since we never created a recursive call to store those values, they are left over from something else.

Lastly, since we know we are in a recursive call, the 0x4C return address must be to the ‘add a0, a0, s0’ instruction right after the recursive call. Additionally, since each call to \texttt{fn} saves 3 words to the stack, each layer of the call has an activation frame of size 3, allowing us to reconstruct the previous activation frames, which are below the current one. We see that the activation frame below the current one also contains the same return address, so it too is a recursive call. However, the frame below that has a different ra, so it must be the frame of the original call to \texttt{fn}.

\begin{itemize}
    \item[(B)] What was the argument to the most recent call to \texttt{fn}?

    \textbf{Most recent argument (HEX):} \texttt{x=_______0x11}

    The argument is moved from s1 to a0 right before the recursive call is made, so that value is also still in s1, since we haven’t modified s1 yet. This means the s1 value saved to the stack is the same as the argument, which in this case is 0x11.

    \item[(C)] What is the missing value marked ??? for the contents of location 1D0?

    \textbf{Contents of 1D0 (HEX):} _______ CAN’T TELL

    We cannot tell what the value of ??? is because those entries are not part of a recursive call to \texttt{fn}, since we haven’t reached the ‘jal ra, fn’ yet. Those values could be leftover from anything, and thus have any random value.

    \item[(D)] What is the hex address of the instruction tagged \texttt{rtn}?

    \textbf{Address of rtn (HEX):} _______ 0x50

    As discussed before, we know that the recursive return address is 0x4C, the address of the ‘add a0, a0, s0’ instruction. We can get the address of the instruction labelled \texttt{rtn}, which
is the very next instruction, by simply adding 4 to this address to get 0x50.

(E)  What was the argument to the first recursive call to fn?

**First recursive call argument (HEX): x=_____0x23**

We were able to use the stack to discover that the lowermost activation frame is that of the original call to fn, which makes the frame above it that of the first recursive call. We can then use our knowledge that the saved s1 value is the same as the argument to find out that the argument to this call was 0x23.

(F)  What is the hex address of the jal instruction that called fn originally?

**Address of original call (HEX): ____0xC0**

The return address that we find in the original call’s stack frame is 0xC4. If this is the address that the original call will eventually return to, then the address of the instruction that made that call would be 4 before it, meaning 0xC4 – 4 = 0xC0

(G)  What were the contents of s1 at the time of the original call?

**Original s1 contents (HEX): ____0x22**

Just like all the recursive calls, the original call saved the value s1 initially had on the stack. By reconstructing the frames for each call, we discovered that this was the 0x22 value.

(H)  What value will be returned to the original caller if the value of a0 at the time of the original call was 0x47?

**Return value for original call (HEX): ____0x4**

Counts the number of 1’s in original number

This problem doesn’t actually rely on the contents of the stack, just understanding what the assembly code is actually doing. As long as x is not 0, the program continues to recurse. Then, as it comes back up the recursive stack, it adds ‘lowbit’ each time, which is 1 if the lowest bit of the current x is 1, with x getting shifted each time. So the program effectively looks at each bit of x and totals how many ones it finds. 0x47 in binary is 0b01000111, which means the program will find 4 ones.
Problem 4. ★

The following C program implements a function \( H(x,y) \) of two arguments, which returns an integer result. The assembly code for the procedure is shown on the right.

```c
int H(int x, int y) {
    int a = x - y;
    if (a < 0) return x;
    else return ???;
}
```

The execution of the procedure call \( H(0x68, 0x20) \) has been suspended just as the processor is about to execute the instruction labeled “rtn:” during one of the recursive calls to \( H \). A partial trace of the stack at the time execution was suspended is shown to the right below.

(A) Examining the assembly language for \( H \), what is the appropriate C code for ??? in the C representation for \( H \)?

\[ \text{C code for ???: \_ \_ \_} \]

Line 2 of the assembly contains a bltz instruction which branches if the value stored in \( t0 \) is less than 0. If this branch is not taken (i.e. \( a > 0 \)) we fall through and continue with the addi instruction. Thus, line 3 in the assembly is the start of the “else” block. We see the stack pointer being decremented by 4 and the return address (ra) being pushed onto the stack with the sw instruction. This is the typical entry sequence in preparation for a function call. Next, an mv instruction copies the value in \( t0 \) into \( a0 \) before calling the function \( H \) (recall that jal \( H \) is the same as the call \( H \) instruction.) By the calling convention, the arguments passed to \( H \) are placed in registers \( a0 \) and \( a1 \). At this point, we see that the value in \( a0 \) is \( t0 \) (from the mv instruction.) \( t0 \) currently contains the value of \( a \). The \( a1 \) register has not been changed and has the same value as when \( H \) was first called. Thus, it contains the second argument passed to \( H \) in the initial (non-recursive) call, so it contains \( y \). The jal \( H \) instruction is therefore calling \( H(a, y) \).

(B) Please fill in the values for the blank locations in the stack dump shown on the right. Express the values in hex or write “---” if value can’t be determined. For all following questions, suppose that during the initial (non-recursive) call to \( H \), sp pointed to the memory location containing \( 0x0010 \).

<table>
<thead>
<tr>
<th>Location</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>sp</td>
<td>0x007c</td>
</tr>
<tr>
<td></td>
<td>0x007c</td>
</tr>
<tr>
<td></td>
<td>0x001c</td>
</tr>
<tr>
<td></td>
<td>0x0010</td>
</tr>
<tr>
<td></td>
<td>0x00e0</td>
</tr>
<tr>
<td></td>
<td>0x00ec</td>
</tr>
<tr>
<td></td>
<td>---</td>
</tr>
</tbody>
</table>
In the initial call to H (let’s call this Call 1), sp starts at the location with 0x0010. As it is about to call H (i.e. just before the jal instruction,) it moves the stack pointer up by 4. Recall that lower memory addresses are drawn at the top of the diagram. Then, it pushes ra onto the stack. We see that this value is 0x001c, which is the value of the ra register during the first call to H. This is the value set by original caller. We don’t know which function called H, but we do know that to return to that function, we can simply jump back to 0x001c. Also, we know that at this point, x = 0x68, y = 0x20, and a = x − y = 0x48. This is greater than 0, so we take the else branch and call H again recursively with H(a, y) = H(0x48, 0x20), (Call 2).

Now, when we call H with the jal instruction, we will overwrite the value in ra with the address of the lw instruction and then jump to the H label. At this point, x = 0x48, y = 0x20, and a = x − y = 0x28. ra currently equals the address of the lw instruction (we don’t know what this is yet.) Once again, a >= 0, so we take the else branch and call H again with H(a, y) = H(0x28, 0x20), (Call 3). To do so, we once again move sp by -4 and push ra onto the stack with the mv instruction. This is the blank slot currently. We don’t know what this is yet. The jal instruction jumps to H and sets ra to the address of the lw instruction.

We repeat the same procedure as above, noting that a = 0x28 – 0x20 = 0x08. This is >= 0, so we take the else branch, move sp by 4, and push ra (the address of the lw instruction.) Observe that this is 0x007c. We now know the address of the lw instruction – it’s 0x007c. This was exactly the same value that was pushed before Call 3. Therefore, the blank slot in the middle of the stack has value 0x007c. Continuing, we call H again with H(0x08, 0x20), (Call 4).

In Call 4, our subtraction produces a negative result, so the bltz instruction jumps to the jr ra instruction and we do not store anything else on the stack. At this point, we will simply be popping off the values on the stack as we return through each of the recursive calls. Therefore, we do not have any additional information about values above 0x007c in the stack. The call to ret jumps us back to ra which points to the lw instruction. This causes us to load the previous ra that was stored on the stack and jump back to that. This continues until we jump back to 0x001c (the ra set by the function that called us in the initial call (Call 1.) Since we do not know what that function does with the stack, we similarly do not have any information about the contents at the bottom of the stack (below 0x00ec).

(C) Determine the specified values at the time execution was suspended. Please express each value in hex or write “CAN’T TELL” if the value cannot be determined.

Value in a0 or “CANT TELL”: 0x _8____________

Value in a1 or “CANT TELL”: 0x _20____________

Value in ra or “CANT TELL”: 0x _7C____________

Value in sp or “CANT TELL”: 0x _CAN’T TELL___

Address of the initial call instruction to H: 0x _0018____

The answers to these questions can be found through the analysis in part (B). Based on the position of sp, we can see that execution was halted while returning from Call 3 as described in the previous section. We have just popped off the top-most 0x007c value on the stack and loaded that into ra. Thus value at ra is 0x7c. At this point, a0 and a1 have not been modified since the final call to H. Thus they contain the values of the final arguments passed to H in Call 4, which
are 0x08 and 0x20 respectively. We have no information about where the stack sits in memory. We only decremented and incremented sp relative to its original value (which is unknown.) Therefore, we do not know the value of sp.

From the analysis in part (B), we know that before we make Call 2, we store the value of ra which is the return address for the function that made Call 1 (the initial call.) This is 4 greater than the address of the actual instruction that called us (since jal links in the next instruction rather than the actual instruction that does the calling.) Thus the address of the instruction that called is us 0x001c – 4 = 0x0018.
From past quizzes:

Problem 4. Stack Detective (16 points)

Below is the Python code for a recursive implementation of binary search, which finds the index at which an element should be inserted into a sorted array to ensure that the array is still sorted after the insertion. To the right is a not so elegant, but valid, implementation of the function using RISC-V assembly.

/* find where to insert element in arr */
unsigned binary_search(int[] arr, 
unsigned start, unsigned end, int element){
    if (start == end){
        return end;
    }
    mid = (start + end) / 2;
    if (element < arr[mid]){ 
        end = mid;
    } else {
        start = mid + 1;
    }
    return binary_search(arr, start, end, element);
}

(A) (2 points) What should be in the blank on the line labeled if to make the assembly implementation match the Python code?

    if: bge _____a3, t1, else_______________

(B) (2 points) How many words will be written to the stack before the program makes each recursive call to the function binary_search?

Number of words pushed onto stack before each recursive call? ____2_____
The program’s initial call to function `binary_search` occurs outside of the function definition via the instruction ‘call binary_search’. The program is interrupted during a recursive call to `binary_search`, just prior to the execution of ‘addi sp, sp, 8’ at label L1. The diagram on the right shows the contents of a region of memory. All addresses and data values are shown in hex. The current value in the SP register is 0xEB0 and points to the location shown in the diagram.

(C) (4 points) What were the values of arguments arr and end at the beginning of the initial call to `binary_search`? Write CAN’T TELL if you cannot tell the value of an argument from the stack provided.

Arguments at beginning of this call:  
arr = 0x___ CAN’T TELL ___  
end = 0x___ A ____________

(D) (4 points) What are the values in the following registers right when the execution of `binary_search` is interrupted? Write CAN’T TELL if you cannot tell.

Current value of s0: 0x____ 6 ____________
Current value of ra: 0x____ C4 ____________

(E) (2 points) What is the hex address of the ‘call binary_search’ instruction that made the initial call to `binary_search`?

Address of instruction that made initial call to binary_search: 0x____ CA0 ________

(F) (2 points) What is the hex address of the `ret` instruction?

0xC4 is address of mv s0, a0. Add 4 for each instruction until you reach ret which is at 0xD8.

Address of `ret` instruction: 0x____ D8 ________